

1) Convert  $r = 3 \cos(\theta)$  to rectangular form.

2) Multiply both sides by  $r$ :

2a)  $r \cdot r = r \cdot 3 \cdot \cos(\theta)$  setup the multiplication

2b)  $r^2 = 3 r \cos(\theta)$  complete the multiplication

3) Replace  $r \cos(\theta)$  with  $x$  and  $r^2$  with  $x^2 + y^2$

$$x^2 + y^2 = 3x$$

4) Move the  $3x$  to the left with subtraction

$$x^2 - 3x + y^2 = 0$$

5) Complete the square on the left.

$$\left(x - \frac{3}{2}\right)^2 - \frac{9}{4} + y^2 = 0$$

1) Complete the square means

rewrite  $x^2 - 3x$  as

$$\left(x - \frac{3}{2}\right)^2 - \frac{9}{4}$$

6) Move the  $-\frac{9}{4}$  to the right side.

$$\left(x - \frac{3}{2}\right)^2 + y^2 = \frac{9}{4}$$

7) Identify this as a circle centered at  $\left(\frac{3}{2}, 0\right)$  with radius  $\sqrt{\frac{9}{4}} = \frac{3}{2}$