

Find the derivative of  $\ln(\sqrt{x+2})$

1) First rewrite the function using a rule of logs.

$$f(x) = \ln((x+2)^{\frac{1}{2}}) \quad \text{Rewrite the root using an exponent}$$

$$f(x) = \frac{1}{2} \ln(x+2) \quad \text{Place the } \frac{1}{2} \text{ in front of the } \ln(x+2)$$

2) Now differentiate using the chain rule.

$$f'(x) = \frac{d}{dx} \frac{1}{2} \ln(x+2) \quad \text{Setup the derivative}$$

$$f'(x) = \frac{1}{2} \frac{d}{dx} \ln(x+2) \quad \text{Pull the } \frac{1}{2} \text{ because it's constant}$$

$$f'(x) = \frac{1}{2} \times \frac{1}{x+2} \times \frac{d}{dx} (x+2) \quad \text{Apply the chain rule.}$$

$$f'(x) = \frac{1}{2} \times \frac{1}{x+2} \times 1 \quad \frac{d}{dx} (x+2) = 1$$

$$f'(x) = \frac{1}{2(x+1)} \quad \text{Rewrite}$$