

Find the slope of the tangent to the surface given below at the point $(2,-1)$

1) Given function: $f(x,y) = 3x+3y-4$

2) Differentiate with respect to x : $f_x(x, y) = 3$. As you can see in the picture below, we have to differentiate with respect to x because we're in a plane parallel to the xz plane. In this plane y does not change.

3) Now we evaluate the derivative at the point $(2,-1)$: $f_x(2, -1) = 3$

4) We can say that the slope of the tangent line at the point $(2,-1)$ in the plane $y=-1$ is 3. This plane is parallel to the xz plane.

5) In the picture below, you can see the plane $y=-1$, and the line in this plane.

