

Table of function values and derivative values.

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|---------|------------|---------------|----------------|------------|------------|------------|-------|
| x | -2 | -1 | 0 | 1 | 2 | 3 | Row 1 |
| $f'(x)$ | 4 | $\frac{2}{3}$ | $-\frac{1}{3}$ | -1 | -2 | -4 | Row 2 |
| $g'(x)$ | 4 | $\frac{2}{3}$ | $-\frac{1}{3}$ | -1 | -2 | -4 | Row 3 |
| $h'(x)$ | can't find | -12 | 1 | can't find | can't find | can't find | Row 4 |

a) $g(x) = f(x) - 2$

The derivative of $g(x)$ is $g'(x) = \frac{d}{dx}(f(x) - 2) = \frac{d}{dx}f(x) - \frac{d}{dx}(2) = f'(x)$

This means the third row has the same values as the first row.

b) $h(x) = f(-3x)$. To differentiate this, you have to use the chain rule.

$$1) \quad h'(x) = \frac{d}{dx}f(-3x) = f'(-3x)(-3) = -3f'(-3x) \quad \text{chain rule}$$

$$2) \quad \text{At } x = -2, \text{ we have } h'(-2) = -3f'(-3(-2)) = -3f'(6).$$

We stop here because we don't know $f'(6)$.

$$3) \quad \text{At } x = -1, \text{ we have } h'(-1) = -3f'(-3(-1)) = -3f'(3) = -3(-4) = -12$$

$$4) \quad \text{At } x = 0, \text{ we have } h'(0) = -3f'(0) = -3\left(\frac{-1}{3}\right) = 1$$

5) The other values can't be found, as in 2) above.